

DERIVATIVES AND GRADIENTS	EXPRESSION	MATHEMATICA SYNTAX
	Partial derivatives of $f : \mathbb{R}^n \rightarrow \mathbb{R}$ $f_x = \frac{\partial f}{\partial x}$ $f_y = \frac{\partial f}{\partial y}$	$D[f[x,y], x]$ or $D[f[x,y,z], x]$, etc. $D[f[x,y], y]$ or $D[f[x,y,z], y]$, etc.
	Partial derivatives of $\bar{f} : \mathbb{R}^n \rightarrow \mathbb{R}^m$ $\frac{\partial f_1}{\partial x}$ $\frac{\partial f_2}{\partial x}$	$D[f[x,y][[1]], x]$ or $D[f[x,y,z][[1]], x]$, etc. $D[f[x,y][[2]], x]$ or $D[f[x,y,z][[2]], x]$, etc. (alternatively, compute total derivative using the command given below, and read off the answer)
	Higher-order partial derivatives of $f : \mathbb{R}^n \rightarrow \mathbb{R}$ $f_{xx} = \frac{\partial^2 f}{\partial x^2}$ $f_{yyyy} = \frac{\partial^5 f}{\partial y^5}$ $f_{xy} = \frac{\partial^2 f}{\partial x \partial y}$ $\frac{\partial^{10} f}{\partial x^3 \partial y^2 \partial z^5}$	$D[f[x,y], x, x]$ or $D[f[x,y], \{x, 2\}]$ $D[f[x,y,z], \{y, 5\}]$ $D[f[x,y], x, y]$ $D[f[x,y,z], \{x, 3\}, \{y, 2\}, \{z, 5\}]$
	Total derivative of $\bar{f} : \mathbb{R}^n \rightarrow \mathbb{R}^m$	$D[f[x,y], x, y]$ or $D[f[x,y,z], \{\{x,y,z\}\}]$, etc. (to get the answer as matrix, click MatrixForm)
	Total derivative of $\bar{f} : \mathbb{R} \rightarrow \mathbb{R}^m$	$f'[x]$ or $f'[t]$, etc. ($f''[x]$ and $f''[x]$ do the obvious things)
	Gradient ∇f	$\text{Grad}[f[x,y], \{x,y\}]$ or $\text{Grad}[f[x,y,z], \{x,y,z\}]$, etc. (or use total derivative command given above)
	Directional derivative $D_{\mathbf{u}} f(\mathbf{x})$	$\text{Grad}[f[x,y], \{x,y\}].\text{Normalize}[u]$ or $\text{Grad}[f[x,y,z], \{x,y,z\}].\text{Normalize}[u]$
	Hessian Hf	$D[f[x,y], \{\{x,y\}, 2\}]$ or $D[f[x,y,z], \{\{x,y,z\}, 2\}]$, etc.
	Jacobian $J(\bar{f}) = \det D\bar{f}$	$\text{Det}[D[f[x,y], \{\{x,y\}\}]]$ or $\text{Det}[D[f[x,y,z], \{\{x,y,z\}\}]]$, etc.

To substitute numerical values for x , y and z , do one of two things:

1. Define the derivative as a function of x , y and z , then ask *Mathematica* to plug in the values of x , y and z to your newly-defined function:

Example: Suppose you wanted to compute $f_{xy}(3, 2, -5)$. You could execute these commands, one at a time:

```
h[x_,y_,z_] = D[f[x,y,z], x, y]
h[3,2,-5]
```

2. Follow any of the commands above with some syntax that causes *Mathematica* to substitute in numbers for the variables:

Example: Suppose you wanted to compute $f_{xy}(3, 2, -5)$. You could execute this single command:

```
D[f[x,y,z], x, y] /.x->3 /.y->2 /.z->-5
```

In general, you follow the command with a series of `/.var->number` commands; this plugs in *number* to variable *var* in the preceding expression.